

Федеральное государственное автономное образовательное

учреждение высшего образования

«Национальный исследовательский университет ИТМО»

Факультет программной инженерии и компьютерной техники

Направление подготовки: 09.03.04 – Системное и прикладное программное обеспечение

Дисциплина «Дискретная математика»

**Отчёт по домашней работе №1**

Вариант №7

Выполнил

Галак Екатерина Анатольевна,

P3115

Проверил

Поляков Владимир Иванович

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# Задание:

## Задание 1 (представление чисел с фиксированной и плавающей запятой в различных форматах)

**1) Заданное число A представить в виде двоично-кодированного числа:**

**а) в упакованном виде (BCD);**

**б) в неупакованном виде (ASCII).**

A = 700 (Вариант №7)

1.а)

|  |  |
| --- | --- |
| 0000.0111 | 0000.0000 |

7 0 0

1.б)

|  |
| --- |
| 0011.0111 |

7

|  |
| --- |
| 0011.0000 |

0

|  |
| --- |
| 0011.0000 |

0

Старшая тетрада байта имеет стандартное значение 0011.

**2) Заданное число A и –A представить в форме с фиксированной запятой.**

2.1. A = (700)10 = (1010111100)2

|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- |
| 0 | 0 | 0 | 0 | 0 | 0 | 1 | 0 | 1 | 0 | 1 | 1 | 1 | 1 | 0 | 0 |
| 15 | 14 | 13 | 12 | 11 | 10 | 9 | 8 | 7 | 6 | 5 | 4 | 3 | 2 | 1 | 0 |

В шестнадцатеричной СС:

(0010)2 = (2)16

(1011)2 = (B)16

(1100)2 = (C)16

(700)10 = (2BC)16

2.2. –A = -70010

Прямой код:

|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- |
| 1 | 0 | 0 | 0 | 0 | 0 | 1 | 0 | 1 | 0 | 1 | 1 | 1 | 1 | 0 | 0 |
| 15 | 14 | 13 | 12 | 11 | 10 | 9 | 8 | 7 | 6 | 5 | 4 | 3 | 2 | 1 | 0 |

Обратный код:

|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- |
| 1 | 1 | 1 | 1 | 1 | 1 | 0 | 1 | 0 | 1 | 0 | 0 | 0 | 0 | 1 | 1 |
| 15 | 14 | 13 | 12 | 11 | 10 | 9 | 8 | 7 | 6 | 5 | 4 | 3 | 2 | 1 | 0 |

Дополнительный код:

|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- |
| 1 | 1 | 1 | 1 | 1 | 1 | 0 | 1 | 0 | 1 | 0 | 0 | 0 | 1 | 0 | 0 |
| 15 | 14 | 13 | 12 | 11 | 10 | 9 | 8 | 7 | 6 | 5 | 4 | 3 | 2 | 1 | 0 |

**3) Заданные числа A и B представить в форме с плавающей запятой в формате Ф1.**

A = 700

B = 0,003

3.1. A = (700)10 = (2BC)16 = (0,2BC)16 \* 163

XA = PA + 64 = 3 + 64 = (67)10 = (1000011)2

|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- |
| 0 | 1 | 0 | 0 | 0 | 0 | 1 | 1 | 0 | 0 | 1 | 0 | 1 | 0 | 1 | 1 | 1 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 | 21 | 22 | 23 | 24 | 25 | 26 | 27 | 28 | 29 | 30 | 31 |

3.2. B = (0,003)10 = (0,00C49BA5E)16 = (0,00C49BA6)16

B = (0,00C49BA6)16 = (0, C49BA6)16 \* 16-2

XB = PB + 64 = -2 + 64 = 62 = (0111110)2

|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- |
| 1 | 0 | 1 | 1 | 1 | 1 | 1 | 0 | 1 | 1 | 0 | 0 | 0 | 1 | 0 | 0 | 1 | 0 | 0 | 1 | 1 | 0 | 1 | 1 | 1 | 0 | 1 | 0 | 0 | 1 | 1 | 0 |
| 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 | 21 | 22 | 23 | 24 | 25 | 26 | 27 | 28 | 29 | 30 | 31 |

**4) Заданные числа A и B представить в форме с плавающей запятой в формате Ф2.**

A = 700

B = 0,003

4.1. A = (700)10 = (2BC)16 = (1010111100)2 = (0,10101111)2 \* 210

XA = PA + 128 = 10 + 128 = 138 = (10001010)2

|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- |
| 0 | 1 | 0 | 0 | 0 | 1 | 0 | 1 | 0 | 0 | 1 | 0 | 1 | 1 | 1 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 31 | 30 | 29 | 28 | 27 | 26 | 25 | 24 | 23 | 22 | 21 | 20 | 19 | 18 | 17 | 16 | 15 | 14 | 13 | 12 | 11 | 10 | 9 | 8 | 7 | 6 | 5 | 4 | 3 | 2 | 1 | 0 |

4.2. B = (0,003)10 = (0,00C49BA6)16 = (0,0000 0000 1100 0100 1001 1011 1010 0110)2 = (0, 1100 0100 1001 1011 1010 011)2 \* 2-8

XB = PB + 128 = -8 + 128 = 120 = (0111 1000)2

|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- |
| 0 | 0 | 1 | 1 | 1 | 1 | 0 | 0 | 0 | 1 | 0 | 0 | 0 | 1 | 0 | 0 | 1 | 0 | 0 | 1 | 1 | 0 | 1 | 1 | 1 | 0 | 1 | 0 | 0 | 1 | 1 | 0 |
| 31 | 30 | 29 | 28 | 27 | 26 | 25 | 24 | 23 | 22 | 21 | 20 | 19 | 18 | 17 | 16 | 15 | 14 | 13 | 12 | 11 | 10 | 9 | 8 | 7 | 6 | 5 | 4 | 3 | 2 | 1 | 0 |

**5) Заданные числа A и B представить в форме с плавающей запятой в формате Ф3.**

5.1) A = (700)10 = (2BC)16 = (1010111100)2 = (1,0101111)2 \* 29

XA = PA + 127 = 9 + 127 = 136 = (10001000)2

|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- |
| 0 | 1 | 0 | 0 | 0 | 1 | 0 | 0 | 0 | 0 | 1 | 0 | 1 | 1 | 1 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 31 | 30 | 29 | 28 | 27 | 26 | 25 | 24 | 23 | 22 | 21 | 20 | 19 | 18 | 17 | 16 | 15 | 14 | 13 | 12 | 11 | 10 | 9 | 8 | 7 | 6 | 5 | 4 | 3 | 2 | 1 | 0 |

5.2) B = (0,003)10 = (0,00C49BA6)16 = (0,0000 0000 1100 0100 1001 1011 1010 0110)2 = (1,100 0100 1001 1011 1010 011)2 \* 2-9

XB = PB + 127 = 118 = (01110110)2

|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- |
| 0 | 0 | 1 | 1 | 1 | 0 | 1 | 1 | 0 | 1 | 0 | 0 | 0 | 1 | 0 | 0 | 1 | 0 | 0 | 1 | 1 | 0 | 1 | 1 | 1 | 0 | 1 | 0 | 0 | 1 | 1 | 0 |
| 31 | 30 | 29 | 28 | 27 | 26 | 25 | 24 | 23 | 22 | 21 | 20 | 19 | 18 | 17 | 16 | 15 | 14 | 13 | 12 | 11 | 10 | 9 | 8 | 7 | 6 | 5 | 4 | 3 | 2 | 1 | 0 |

**6) Найти значение чисел Y и Z по их заданным шестнадцатеричным представлениям R и S в форме с плавающей точкой в формате Ф1.**

R = 419A0000

S = BF600000

6.1) Для определения значения числа Y производится наложение его шестнадцатеричного представления R на разрядную сетку формата Ф1:

|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- |
| 0 | 1 | 0 | 0 | 0 | 0 | 0 | 1 | 1 | 0 | 0 | 1 | 1 | 0 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 | 21 | 22 | 23 | 24 | 25 | 26 | 27 | 28 | 29 | 30 | 31 |

Из этого представления видно, что число Y – положительное (в знаковом разряде числа – ноль).

Определим порядок числа Y по его характеристике:

XY = (1000001)2 = 6510 = 64 + 1, где 64 – смещение, а 1 – порядок

PY = XY – 64 = 1

Представим число Y с помощью мантиссы и порядка:

Y = (0,9A)16 \* 161

Получили представление числа в нормальной (полулогарифмической) форме. Для приведения числа Y к естественной форме необходимо перенести запятую в мантиссе на количество шестнадцатеричных цифр, равное модулю порядка, вправо – при положительном или влево – при отрицательном порядке.

Y = (9,A)16

Переведем число Y из шестнадцатеричной системы счисления в десятичную:

Y = (9,A)16 = (9,625)10

6.2) Для определения значения числа Z производится наложение его шестнадцатеричного представления S (BF600000) на разрядную сетку формата Ф1:

|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
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| 1 | 0 | 1 | 1 | 1 | 1 | 1 | 1 | 0 | 1 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 | 21 | 22 | 23 | 24 | 25 | 26 | 27 | 28 | 29 | 30 | 31 |

Порядок числа Z:

PZ = XZ – 64 = 63 – 64 = -1

Значение числа Z:

Z = (0,6)16 \* 16-1 = (0,06)16 = 6 \* 16-2 = 6/162 = 6/28 = 3/27 = (3\*23) / 210 = 24 \* (1 / 1024) = 24 \* 10-3 => Z = (0,0024)10

**7)** **Найти значение чисел V и W по их заданным шестнадцатеричным представлениям R и S в форме с плавающей точкой в формате Ф2.**

R = 419A0000

S = BF600000

7.1) Представление числа V в формате Ф2 имеет вид:

|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- |
| 0 | 1 | 0 | 0 | 0 | 0 | 0 | 1 | 1 | 0 | 0 | 1 | 1 | 0 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 31 | 30 | 29 | 28 | 27 | 26 | 25 | 24 | 23 | 22 | 21 | 20 | 19 | 18 | 17 | 16 | 15 | 14 | 13 | 12 | 11 | 10 | 9 | 8 | 7 | 6 | 5 | 4 | 3 | 2 | 1 | 0 |

Порядок числа V:

PV = XV – 128 = 131 – 128 = 3

Значение числа V в нормальной форме:

V = (0,1001101)2 \* 23

При определении двоичного значения мантиссы производится восстановление её скрытого старшего разряда, равного 1.

Для приведения числа V к естественной форме запятая в его мантиссе переносится вправо на 3 двоичных разряда:

V = (10,01101)2 = (2,40625)10

7.2) Представление числа W в формате:

|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- |
| 1 | 0 | 1 | 1 | 1 | 1 | 1 | 1 | 0 | 1 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 31 | 30 | 29 | 28 | 27 | 26 | 25 | 24 | 23 | 22 | 21 | 20 | 19 | 18 | 17 | 16 | 15 | 14 | 13 | 12 | 11 | 10 | 9 | 8 | 7 | 6 | 5 | 4 | 3 | 2 | 1 | 0 |

Порядок числа W:

PW = XW – 128 = 126 – 128 = -2

Число W в нормальной форме:

W = (0,111)2 \* 2-2

Число W в естественной форме получается переносом запятой в мантиссе влево на 2 двоичных разряда:

W = (0,00111)2 = (111)2 \* 2-5 = 7 / 32 = 0,21875

**8)** **Найти значение чисел T и Q по их заданным шестнадцатеричным представлениям R и S в форме с плавающей точкой в формате Ф3.**

R = 419A0000

S = BF600000

8.1) Представление числа T в формате Ф3 имеет тот же вид, что и для числа V в формате Ф2.

|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- |
| 0 | 1 | 0 | 0 | 0 | 0 | 0 | 1 | 1 | 0 | 0 | 1 | 1 | 0 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 31 | 30 | 29 | 28 | 27 | 26 | 25 | 24 | 23 | 22 | 21 | 20 | 19 | 18 | 17 | 16 | 15 | 14 | 13 | 12 | 11 | 10 | 9 | 8 | 7 | 6 | 5 | 4 | 3 | 2 | 1 | 0 |

Порядок числа T:

PT = XT – 127 = 131 – 127 = 4

Значение числа T в двоичной СС:

T = (1,001101)2 \* 24 = 1,203125 \* 16 = 19,25

8.2) Представление числа Q в формате Ф3 имеет тот же вид, что и для числа в Ф2.

|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- |
| 1 | 0 | 1 | 1 | 1 | 1 | 1 | 1 | 0 | 1 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 31 | 30 | 29 | 28 | 27 | 26 | 25 | 24 | 23 | 22 | 21 | 20 | 19 | 18 | 17 | 16 | 15 | 14 | 13 | 12 | 11 | 10 | 9 | 8 | 7 | 6 | 5 | 4 | 3 | 2 | 1 | 0 |

Порядок числа Q:

PQ = XQ – 127 = 126 – 127 = -1

Значение числа Q:

Q = (1,11)2 \* 2-1 = (111)2 \* 2-3 = 7 / 8 = 0,875